

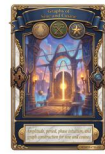
# Graphs of Sine and Cosine

Amplitude, period, phase intuition, and graph construction for sine and cosine.

Name \_\_\_\_\_ Date \_\_\_\_\_

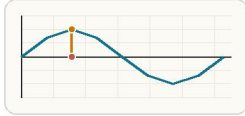
32 main 2-up grid 2 pages

### Completion Reward



Shown here as a small pack artifact, not a preview destination.

1. What does amplitude measure on a sine or cosine graph?



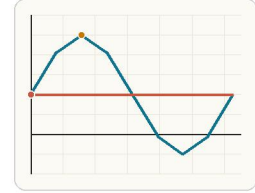
Amplitude is the vertical size of the wave from its midline up to a maximum or down to a minimum.

- A. The x-value of the first intercept
- B. The total width of the graph
- C. The distance from the midline to a peak
- D. The slope at the origin

2. What does period measure on a sine or cosine graph?

- A. The horizontal length of one full cycle
- B. The highest y-value only
- C. The vertical distance between peaks
- D. The y-intercept

3. What is the midline of  $y = 3\sin(x) + 2$ ?



In  $y = 3\sin(x) + 2$ , the +2 moves the whole graph up, so the midline is  $y = 2$ .

- A.  $y = 3$
- B.  $x = 2$
- C.  $x = 3$
- D.  $y = 2$

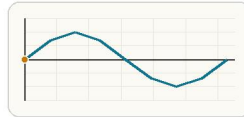
4. What value does  $y = \cos(x)$  have at  $x = 0$ ?



The basic cosine graph starts at  $y = 1$  when  $x = 0$ .

- A. 0
- B. -1
- C. 1
- D.  $2\pi$

5. What value does  $y = \sin(x)$  have at  $x = 0$ ?



The basic sine graph passes through the midline at  $x = 0$ , so its value there is 0.

- A. 1
- B. -1
- C.  $2\pi$
- D. 0

6. What is the amplitude of  $y = 4\cos(x)$ ?

- A. 1
- B.  $2\pi$
- C. 4
- D. 0

7. What is the period of  $y = \sin(x)$ ?

- A.  $\pi$
- B.  $4\pi$
- C. 1
- D.  $2\pi$

8. What is the period of  $y = \cos(x)$ ?

- A.  $\pi$
- B.  $4\pi$
- C. 1
- D.  $2\pi$

9. Which equation has amplitude 3?

- A.  $y = \sin(3x)$
- B.  $y = 3\sin(x)$
- C.  $y = \sin(x) + 3$
- D.  $y = \cos(x / 3)$

10. Which equation has midline  $y = 2$ ?

- A.  $y = 2\sin(x)$
- B.  $y = \sin(2x)$
- C.  $y = \sin(x) + 2$
- D.  $y = 2\cos(2x)$

11. Which equation has period  $\pi$ ?

- A.  $y = \sin(2x)$
- B.  $y = \sin(x)$
- C.  $y = \sin(x / 2)$
- D.  $y = 2\sin(x)$

12. Which basic graph starts at a maximum when  $x = 0$ ?

- A.  $y = \cos(x)$
- B.  $y = \sin(x)$
- C.  $y = \tan(x)$
- D.  $y = x$

13. Which basic graph starts at 0 when  $x = 0$ ?

- A.  $y = \cos(x)$
- B.  $y = \sin(x)$
- C.  $y = \sec(x)$
- D.  $y = x^2$

14. What is the best first step when reading a transformed sine graph?

- A. Compute a derivative.
- B. Square the equation.
- C. Look only at the x-intercepts.
- D. Find the midline and amplitude.

15. A student says  $y = \sin(3x)$  has period  $6\pi$ . What is the mistake?

- A. The inside factor 3 makes the period shorter, not longer.
- B. Sine graphs never have periods.
- C. The period should be  $3\pi$  because of the coefficient.
- D. The graph should be treated as linear.

16. What is the amplitude of  $y = -5\sin(x)$ ? Answer with a number.

17. What is the amplitude of  $y = 2\cos(x) - 3$ ? Answer with a number.

18. Find  $y$  when  $y = 3\sin(x)$  and  $x = 0$ . Answer with a number.

19. Find  $y$  when  $y = 4\cos(x)$  and  $x = 0$ . Answer with a number.
20. Find the midline value of  $y = 2\sin(x) + 5$ . Answer with a number.
21. What is the maximum value of  $y = 3\sin(x) + 1$ ? Answer with a number.
22. What is the minimum value of  $y = 3\sin(x) + 1$ ? Answer with a number.
23. What is the period of  $y = \sin(2x)$ ? Answer with a number.
24. Which student correctly finds the amplitude of  $y = -4\cos(x) + 1$ ?
- A. Student B: the amplitude is  $-4$  because the coefficient is negative.  
B. Student A: the amplitude is  $4$  because amplitude uses absolute value.  
C. Student C: the amplitude is  $1$  because of the vertical shift.  
D. Student D: the amplitude is  $5$  because  $-4 + 1 = -3$ .
25. Write an equation with amplitude  $3$  and no vertical shift using sine. Answer in the form  $y = \dots$
26. Write an equation with amplitude  $2$  and no vertical shift using cosine. Answer in the form  $y = \dots$
27. Write an equation with amplitude  $1$  and midline  $y = 4$  using sine. Answer in the form  $y = \dots$
28. Write an equation with amplitude  $5$  and midline  $y = -2$  using cosine. Answer in the form  $y = \dots$
29. Write an equation with sine period  $\pi$ . Answer in the form  $y = \dots$
30. Write an equation with cosine period  $\pi$ . Answer in the form  $y = \dots$
31. For  $y = 4\sin(x) - 1$ , state the midline. Answer as an equation.
32. For  $y = 2\cos(x) + 3$ , state the maximum value as an equation in  $y$ .